

$$2 - \frac{3}{x+4} = \frac{12}{x^2+4x}$$

~~$x(x+4)$~~
 ~~$x(x+4)$~~
 ~~$x(x+4)$~~

ex. values

$$x \neq -4$$

$$x \neq 0$$

LCD

$$1 \cdot (x+4) \cdot x$$

$$2x(x+4) - 3x = 12$$

$$2x^2 + 8x - 3x = 12$$

$$2x^2 + 5x - 12 = 0$$

$$\cancel{(2x+8)(2x-3)} = 0$$

$$(x+4)(2x-3) = 0$$

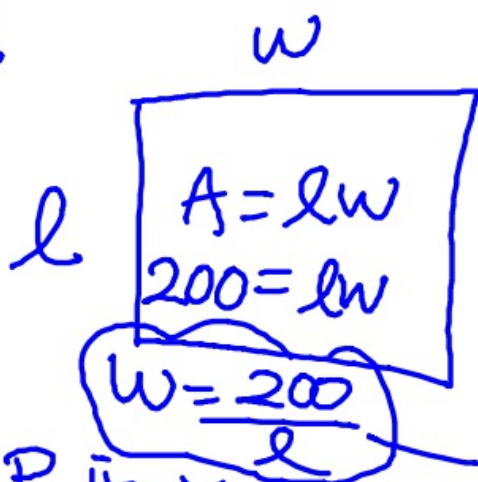
$$x+4 = 0 \quad 2x-3 = 0$$

~~$x = -4$~~

$$x = \frac{3}{2}$$

$$\begin{array}{r} -24 \\ 8 \times 3 \\ \hline 24 \\ \hline -3 \end{array}$$

40.



$$A = 200 \text{ m}^2$$

$$x = l$$

$$a) P = 2l + 2w$$

$$a) P \text{ in } x$$

$$P = 2l + 2\left(\frac{200}{l}\right)$$

$$b) \text{ dims } P = 70 \text{ m}$$

$$l \cdot 70 = 2l + \frac{400}{l}$$

$$70l = 2l^2 + 400$$

$$0 = 2l^2 - 70l + 400$$

$$0 = (2l + 80)(2l - 10)$$

$$l = x = \frac{70 \pm \sqrt{4900 - 4(2)(400)}}{4}$$

$$l = + \text{ m}$$

15

$$\frac{(x-3) \cancel{x(x+1)}}{\cancel{x}} - \frac{3 \cancel{x(x+1)}}{\cancel{x+1}} + \frac{3 \cancel{x(x+1)}}{x^2+x} = 0$$

$x(x+1)$

ex. val

$x \neq 0$

$x \neq -1$

LCD

$x(x+1)$

$$(x-3)(x+1) - 3x + 3 = 0$$

$$x^2 - 2x - 3 - 3x + 3 = 0$$

$$x^2 - 5x = 0$$

$$x(x-5) = 0$$

~~$x=0$~~

$x=5$

$$30. \quad x \cdot \frac{x^2}{1} - \frac{3 \cdot x}{x} = \frac{7 \cdot x}{1}$$

ex. val.

$$x \neq 0$$

$$x^3 - 3 = 7x$$

$$x^3 - 7x - 3 = 0$$

LCD

x

$$x = -2.4$$

$$x = -0.4$$

$$x = 2.8$$

$$18. \quad \frac{x+3}{x} - \frac{2x}{x+3} = \frac{6}{x^2+3x}$$

~~$x(x+3)$~~ ~~$x(x+3)$~~ ~~$x(x+3)$~~

ex val

$$x \neq 0$$

$$x \neq -3$$

LCD

$$x(x+3)$$

$$(x+3)(x+3) - 2x = 6$$

$$x^2 + 4x + 9 - 6 = 0$$

$$x^2 + 4x + 3 = 0$$

$$(x+3)(x+1) = 0$$

~~$x = -3$~~

$$x = -1$$

Varies directly

The amount of confusion about a math topic is proportional to the percent of time a student spends sleeping during lesson.

$$y = kx$$

$$C = kS$$

$$57 = k(75)$$

$$k = \frac{57}{75}$$

$$k = .8$$

A student that sleeps 75% of the time is confused by 57 scale.

What % of time was

spent sleeping if scale for conf. is 38.

$$C = .8S$$

$$\frac{38}{.8} = \frac{.8S}{.8}$$

$$S = 47\%$$

~~At~~ Income is inversely proportional to the # of years spent in college.

$$I = \frac{k}{C}$$

$$40000 = \frac{k}{7}$$

$$280000 = k$$

$$I = \frac{280000}{10}$$

Finding Complex zeros

$$2x^4 + 5x^3 - x^2 + 5x - 3$$

1. put in $y =$ & find a zero

$$\begin{array}{r} -3 \overline{) 2 \quad 5 \quad -1 \quad 5 \quad -3} \\ \underline{-6 \quad 3 \quad -6 \quad 3} \\ 2 \quad -1 \quad 2 \quad -1 \quad \underline{0} \end{array}$$

$$x^4 - x^3 - 7x^2 + 6x + 8$$

$$\begin{array}{r|rrrrr} 2 & 1 & -1 & -7 & 6 & 8 \\ & & 2 & 2 & -10 & -8 \\ \hline \# & 1 & 1 & -5 & -4 & 0 \end{array}$$

$$\hline \begin{array}{r|rr} x & 1 & -12 \\ \hline & & 0 \end{array}$$

$$x^2 - x - 12 = 0$$

$$\begin{array}{r}
 \underline{1+i} \mid 1 \quad -2 \quad -1 \quad 6 \quad -6 \\
 \phantom{\underline{1+i} \mid} \quad 1+i \quad -2 \quad -3-3i \quad 6 \\
 \hline
 \underline{1-i} \mid 1 \quad -1+i \quad -3 \quad 3-3i \\
 \phantom{\underline{1-i} \mid} \quad 1-i \quad 0 \quad -3+3i \\
 \hline
 \phantom{\underline{1-i} \mid} \quad 0 \quad -3 \quad \underline{0}
 \end{array}$$

$$x^2 - 3 = 0$$

$$x = \pm \sqrt{3}$$

$$f(x) = \frac{(x-1)(x+3)}{(x+3)(x-4)}$$

D: $(-\infty, -3) \cup (-3, 4) \cup (4, \infty)$
 R: $(-\infty, \frac{4}{7}) \cup (\frac{4}{7}, 1) \cup (1, \infty)$

hole: $(-3, \frac{4}{7})$

SA: none

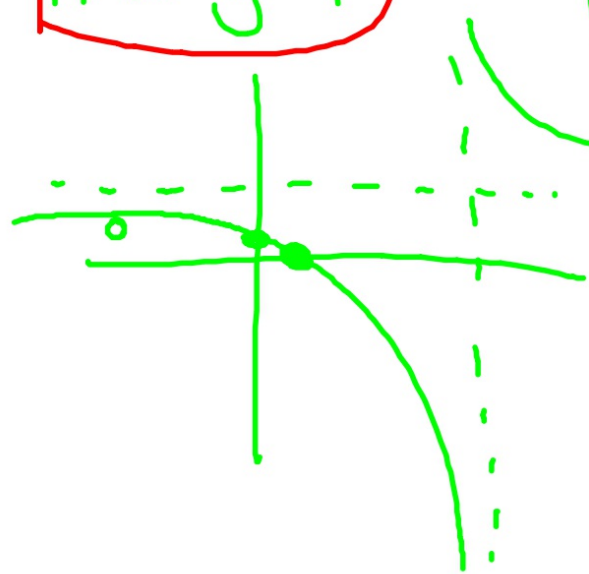
VA: $x=4$

x-int: $x-1=0$

HA: $y=1$

$(1, 0)$

y-int: $\frac{0-1}{0-4} = (0, \frac{1}{4})$



$$27. \quad \frac{4x \cancel{(x+4)(x-1)}}{\cancel{x+4}} + \frac{5 \cancel{(x+4)(x-1)}}{\cancel{x-1}} = \frac{15 \cancel{(x+4)(x-1)}}{\cancel{x^2+3x-4} \cancel{(x+4)(x-1)}}$$

ex val

$$x \neq -4$$

$$x \neq 1$$

LCD

$$(x+4)(x-1)$$

$$4x(x-1) + 5(x+4) = 15$$

$$4x^2 - 4x + 5x + 20 - 15 = 0$$

$$4x^2 + x + 5 = 0$$

$$\begin{array}{r} 20 \\ -5 \times -4 \\ \hline 1 \end{array}$$

$$x = \frac{-1 \pm \sqrt{1 - 4(4)(5)}}{8}$$

$$x = \frac{-1 \pm \sqrt{-79}}{8}$$

No Soln

$$30. \quad x \frac{x^2}{1} - \frac{3}{x} x = \frac{7}{1} x$$

$x \neq 0$
LCD: x

$$x^3 - 3 = 7x$$

$$x^3 - 7x - 3 = 0$$

$$\textcircled{39} \quad \frac{1}{x} = \frac{1}{2.3} + \frac{1}{y}$$

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$\frac{1}{R} = \frac{x \cdot 1}{x \cdot 2.3} + \frac{1 \cdot 2.3}{x \cdot 2.3}$$

a) as x

b) $R = 1.7, x = ?$

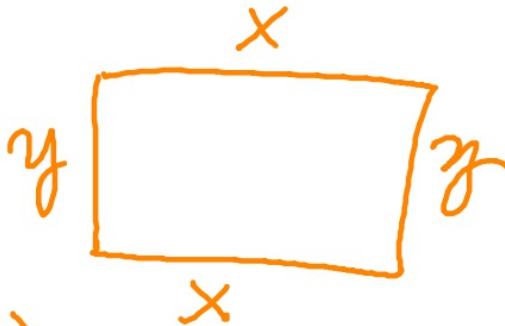
$$\frac{1}{R} = \frac{x+2.3}{2.3x}$$

$$R = \frac{2.3x}{x+2.3}$$

$$\frac{1.7}{1} = \frac{2.3x}{x+2.3}$$

$$1.7(x+2.3) = 2.3x$$

40.



$$l = x$$

$$A = 200 \text{ m}^2$$

$$xy = 200$$

$$y = \frac{200}{x}$$

$$a) P(x) = 2x + 2y$$

$$P(x) = 2x + 2 \left(\frac{200}{x} \right)$$

$$P(x) = 2x + \frac{400}{x}$$

$$b) x \cdot 70 = \frac{2x^2}{1} + \frac{400}{x} \cdot x$$

$$70x = 2x^2 + 400$$

$$= 2x^2 - 70x + 400$$

$$x = \frac{70 \pm \sqrt{4900 - 4(2)(400)}}{4}$$

$$x = 27.8$$

$$y =$$

$$x = 7.2$$

$$y =$$

$$f(x) = \frac{4x}{x^3 - 9x}$$

~~$$\begin{array}{r} -30 \\ -6 \quad 5 \\ -1 \end{array}$$~~

④

$$\frac{8x^2 + 26x + 15}{2x^2 - x - 15}$$

$\frac{120}{6 \cdot 20}$

$$(8x+6)(8x+20)$$

$$(2x-6)(2x+5)$$

$$f(x) = \frac{(4x+3)(2x+5)}{(x-3)(2x+5)}$$

hole: $(-\frac{5}{2}, \frac{3}{11})$

$$\left. \begin{array}{l} 2x+5=0 \\ x=-\frac{5}{2} \end{array} \right\} \begin{array}{l} 4(-\frac{5}{2})+3 \\ -\frac{5}{2}-3 \end{array}$$

VA: $x-3=0$

$$\boxed{x=3}$$

$$\boxed{HA: y=4}$$

x-int $4x+3=0$

$$x = -\frac{3}{4}$$

$$\left(-\frac{3}{4}, 0\right)$$

y-int $\frac{4(0)+3}{0-3} = -1$

$$\boxed{(0, -1)}$$

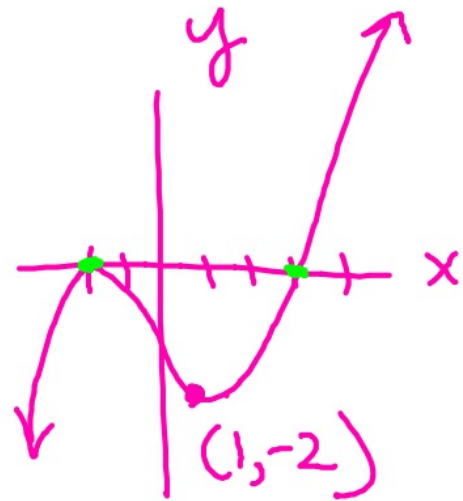
$$f(x) = \frac{x^3 + 8}{x^2 - x - 6}$$

$$\frac{(x+2)(x^2 - 2x + 4)}{(x-3)(x+2)}$$

$$3x^4 - 4x^3 + 7x^2 - 10x + 12$$

$$3, \pm 6i,$$

$$x=3 \quad x=6i \quad x=-6i$$
$$(x-3)(x-6i)(x+6i)$$



$$y = a(x+2)(x+2)(x-3)$$

$$-2 = a(1+2)(1+2)(1-3)$$

$$-2 = -18a$$

$$a = \frac{1}{9}$$

$$y = \frac{1}{9}(x+2)(x+2)(x-3)$$

$$\begin{array}{r}
 4x - 17 + \frac{57x - 24}{x^2 + 3x - 1} \\
 \hline
 x^2 + 3x - 1 \overline{) 4x^3 - 5x^2 + 2x - 7} \\
 \underline{- 4x^3 + 12x^2 - 4x} \\
 17x^2 + 6x - 7 \\
 \underline{+ 17x^2 + 51x - 17} \\
 \hline
 57x - 24
 \end{array}$$